How to Specify it!

A guide to writing properties of pure functions.

John Hughes

Imagine testing **reverse**...

Imagine testing **reverse**... with QuickCheck

Replicating the code in the tests...

Expensive!

Low value!

What can we do instead?

prop_Reverse :: [Int] -> Property prop_Reverse xs = reverse (reverse xs) === xs

> *Check a property of the return value instead*

***Reverse>** quickCheck prop_Reverse +++ OK, passed 100 tests.

***Reverse>** quickCheck test_Reverse *** Failed! Falsified (after 1 test): $\lceil 1, 2, 3 \rceil$ /= $\lceil 3, 2, 1 \rceil$

prop_Wrong :: [Int] -> Property prop_Wrong xs = reverse xs === xs

***Reverse>** quickCheck prop_Wrong *** Failed! Falsified (after 3 tests and 3 shrinks): $\boxed{0,1}$ \leftarrow [1,0] /= [0,1] *Counterexample: Almost always [0,1], sometimes [1,0]*

Shrinking

- Discards unnecessary list elements (we need at least two)
- Replaces integers by smaller integers (we need *distinct* integers, {0,1} are the two smallest)

Property Based Testing

- Random generation of *lots* of test cases
- Shrinking results in *minimal* counterexamples—easy to debug

• *Replicating code in the tests* is tempting, but expensive, and low value

toList :: BST k v -> [(k, v)] keys :: BST k v -> [k]

Generator and shrinker

instance (Ord k, Arbitrary k, Arbitrary v) => Arbitrary (BST k v) where

-- shrinker

shrink = genericShrink

Shrink using a generic QuickCheck mechanism

Is there an *invariant*?

valid :: Ord k => BST k v -> Bool

```
valid Leaf = True
```

```
valid (Branch l k v r) =
  valid l && valid r &&
  all (<k) (keys l) && all (>k) (keys r)
```
Invariant properties

prop_NilValid = valid (nil :: Tree)

prop_InsertValid :: Key -> Val -> Tree -> Bool prop_InsertValid k v t = valid (insert k v t)

prop_DeleteValid :: Key -> Tree -> Bool prop_DeleteValid k t = valid (delete k t)

prop_UnionValid :: Tree -> Tree -> Bool prop_UnionValid t t' = valid (union t t')

> **type Key = Int type Val = Int type Tree = BST Key Val**


```
=== prop_InsertValid from BSTSpec.hs:19 ===
*** Failed! Falsified (after 6 tests and 8 shrinks):
0
0
Branch Leaf 0 0 Leaf
=== prop_DeleteValid from BSTSpec.hs:22 ===
*** Failed! Falsified (after 8 tests and 7 shrinks):
0
Branch Leaf 1 0 (Branch Leaf 0 0 Leaf)
=== prop_UnionValid from BSTSpec.hs:25 ===
*** Failed! Falsified (after 7 tests and 9 shrinks):
Branch Leaf 0 0 (Branch Leaf 0 0 Leaf)
Leaf
```


```
=== prop_InsertValid from BSTSpec.hs:19 ===
*** Failed! Falsified (after 6 tests and 8 shrinks):
0
0
Branch Leaf 0 0 Leaf
=== prop_DeleteValid from BSTSpec.hs:22 ===
*** Failed! Falsified (after 8 tests and 7 shrinks):
0
Branch Leaf 1 \triangleright (Branch Leaf 0 \triangleright Leaf)
=== prop_UnionValid from BSTSpec.hs:25 ===
*** Failed! Falsified (after 7 tests and 9 shrinks):
Branch Leaf 0 \beta (Branch Leaf 0 \beta Leaf)
Leaf
```
Testing our tests

prop_ArbitraryValid t = valid t

prop_ShrinkValid t = all valid (shrink t)

Branch Leaf 0 0 (Branch Leaf 0 1 Leaf) → Branch Leaf 0 0 (Branch Leaf 0 0 Leaf)

What is the *postcondition*?

What is the *postconditic*

"After calling **insert**, we should be

able to find the kev inserted, and an able to **find** the key inserted, and any other keys present beforehand"

What is the postcondition of **find**?

"After calling **find**,

—if the key is present in the tree, the result is **Just value**

—if the key is not present, the result is **Nothing**"

How can we tell this?

By construction!

prop_FindPostAbsent k t = find k (delete k t) === Nothing

prop_InsertInsert (k,v) (k',v') t = insert k v (insert k' v' t) === if k==k' then insert k v t else insert k' v' (insert k v t)

=== prop_InsertInsert from BSTSpec.hs:78 === * Failed! Falsified (after 2 tests): (1,0) (0,0) Leaf** Branch Leaf $\overline{0}$ $\overline{0}$ (Branch Leaf $\overline{1}$ $\overline{0}$ Leaf) /=

Branch (Branch Leaf 0 0 Leaf) 1 0 Leaf

Equivalence for trees

t1 =~= t2 = toList t1 === toList t2

```
prop_InsertInsert (k,v) (k',v') t =
  insert k v (insert k' v' t)
  =~=
  if k==k' then insert k v t else
  insert k' v' (insert k v t)
```


Metamorphic Testing

Montréal, QC, Canada

conjunction with ICSE 2019

May 26, 2019


```
prop_InsertModel (k,v) t =
  toList (insert k v t) 
  === 
  L.insert (k,v) (toList t)
```

```
*BSTSpec> quickCheck prop_InsertModel
*** Failed! Falsified (after 13 tests and 7 shrinks):
(1,0)Branch Leaf 1 0 Leaf
[(1,0)] /= [(1,0),(1,0)]duplicated key
```
prop InsertModel (k, v) t = toList (insert k v t) $===$

L.insert (k,v) (deleteKey k \$ toList t)

Acta Informatica 1, 271-281 (1972) © by Springer-Verlag 1972

Proof of Correctness of Data Representations

C. A. R. Hoare

Received February 16, 1972

Summary. A powerful method of simplifying the proofs of program correctness is suggested; and some new light is shed on the problem of functions with side-effects.

1. Introduction

In the development of programs by stepwise refinement $[1-4]$, the programmer is encouraged to postpone the decision on the representation of his data until after he has designed his algorithm, and has expressed it as an "abstract" program operating on "abstract" data. He then chooses for the abstract data some convenient and efficient concrete representation in the store of a computer; and finally programs the primitive operations required by his abstract program in terms of this concrete representation. This paper suggests an automatic method of accomplishing the transition between an abstract and a concrete program, and also a method of proving its correctness; that is, of proving that the concrete representation exhibits all the properties expected of it by the "abstract" pro-

prop_FindPostPresent k v t = find k (insert k v t) === Just v

=== prop_UnionPost from BSTSpec.hs:75 === Mean time to failure: 50.04595404595405

=== prop_InsertUnion from BSTSpec.hs:117 ===

=== prop_DeleteUnion from BSTSpec.hs:145 === Mean time to failure: 4 696303694

=== prop_UnionDeleteInsert from BSTSpec.hs:167 === Mean time to failure: 7 2. 32767233

Mean time to failure
 $=$ prop_DeleteUnion fr

Mean time to failure: 4
 $\overline{0}$
 $=$ $\overline{0}$ prop_UnionDeleteIns

Mean time to failure: 7
 $\overline{1}$ $\overline{0}$ $\overline{0}$ $\overline{0}$ $\overline{0}$ $\overline{0}$
 $\overline{1}$ $\overline{0}$ $\overline{0}$ **=== prop_UnionUnionAssoc from BSTSpec.hs:185 === Mean time to failure: 8.8995104895**

 $=$ **=== prop_FindUnion from BSTS, hs:206 ===** Mean time to failure. **50.2827**

 $==$ prop UnionModel from β ec.hs:290 === Mean time to failure

Mean time to failure: 4

Mean time to failure: 4

Mean time to failure: 7

Mean time to failure: 7

Mean time to failure: 8

Mean time to failure: 8

Mean time to failure: 8

Mean time to failure

Mea

```
prop_UnionPost t t' k =
  find k (union t t')
  ===
  (find k t <|> find k t')
```

```
prop_UnionModel t t' =
  toList (union t t') 
  === 
  List.sort
    (List.unionBy
       ((==) `on` fst)
       (toList t) 
       (toList t'))
```
Mean time to failure

Averaged over seven bugs, and all properties of each type that detect the bugs

Model-based

- Easier to think of than postconditions
- Require fewer properties than metamorphic approach
- Are the most effective properties
- Find bugs fastest
- *Complete* specification

Metamorphic

- *Do not require a model*
- Easiest to write
- Good effectiveness

How to Specify it!

A Guide to Writing Properties of Pure Functions.

John Hughes

Chalmers University of Technology and Quviq AB, Göteborg, Sweden.

Abstract. Property-based testing tools test software against a specification, rather than a set of examples. This tutorial paper presents five generic approaches to writing such specifications (for purely functional code). We discuss the costs, benefits, and bug-finding power of each approach, with reference to a simple example with eight buggy variants. The lessons learned should help the reader to develop effective propertybased tests in the future.

Introduction 1

Property-based testing (PBT) is an approach to testing software by defining general properties that ought to hold of the code, and using (usually randomly) generated test cases to test that they do, while reporting minimized failing tests if they don't. Pioneered by QuickCheck¹ in Haskell [7], the method is now supported by a variety of tools in many programming languages, and is increasingly popular in practice. Searching for "property-based testing" on Youtube finds many videos on the topic—most of the top 100 recorded at developer conferences and meetings, where (mostly) other people than this author present ideas, tools and methods for PBT, or applications that make use of it. Clearly, nnon outre bogged togting is on idea whose time bog comes. Dut courally closuly it is

Michał Pałka Magnus Myreen (Eds.)

LNCS 11457 **Trends in Functional Programming**

19th International Symposium, TFP 200 2019 **Revised Selected Papers**

Just submitted: How to Specify it! A Guide to Writing Properties of Pure Functions. Hope it will prove useful!

 \mathcal{F}

△ □ 后 中 梦 *③* SWE

 $2020 - 02 - 12$

4:35 PM · Jul 4, 2019 · Twitter Web Client

耳i

https://t.co/r5Z4tda5Cn?amp=1

 \equiv

 $20+$