How to Specify it!

A guide to writing properties of pure functions.

John Hughes





Imagine testing **reverse**...





Imagine testing **reverse**... with QuickCheck



Replicating the code in the tests...



Expensive!

Low value!

What can we do instead?

Check a **property** of the return value instead *Reverse> quickCheck prop_Reverse
+++ OK, passed 100 tests.





*Reverse> quickCheck test_Reverse
*** Failed! Falsified (after 1 test):
[1,2,3] /= [3,2,1]

prop Wrong :: [Int] -> Property prop Wrong xs = reverse xs === xs *Reverse> quickCheck prop Wrong *** Failed! Falsified (after 3 tests and 3 shrinks): [0,1] ← [1,0] /= [0,1]Counterexample: Almost always [0,1], sometimes [1,0]

Shrinking

- Discards unnecessary list elements (we need at least two)
- Replaces integers by smaller integers (we need *distinct* integers, {0,1} are the two smallest)

Property Based Testing



- Random generation of *lots* of test cases
- Shrinking results in *minimal* counterexamples—easy to debug



 Replicating code in the tests is tempting, but expensive, and low value





-- auxiliary operations
toList :: BST k v -> [(k, v)]
keys :: BST k v -> [k]

Generator and shrinker

instance (Ord k, Arbitrary k, Arbitrary v) =>
 Arbitrary (BST k v) where



-- shrinker

shrink = genericShrink

Shrink using a generic QuickCheck mechanism



Is there an *invariant*?

```
valid :: Ord k \implies BST k v \implies Bool
```

```
valid Leaf = True
```

```
valid (Branch l k v r) =
valid l && valid r &&
all (<k) (keys l) && all (>k) (keys r)
```

Invariant properties

prop NilValid = valid (nil :: Tree)

prop_InsertValid :: Key -> Val -> Tree -> Bool
prop InsertValid k v t = valid (insert k v t)

prop_DeleteValid :: Key -> Tree -> Bool
prop DeleteValid k t = valid (delete k t)

prop_UnionValid :: Tree -> Tree -> Bool
prop UnionValid t t' = valid (union t t')

type Key = Int
type Val = Int
type Tree = BST Key Val



```
=== prop InsertValid from BSTSpec.hs:19 ===
*** Failed! Falsified (after 6 tests and 8 shrinks):
0
0
Branch Leaf 0 0 Leaf
=== prop DeleteValid from BSTSpec.hs:22 ===
*** Failed! Falsified (after 8 tests and 7 shrinks):
0
Branch Leaf 1 0 (Branch Leaf 0 0 Leaf)
=== prop UnionValid from BSTSpec.hs:25 ===
*** Failed! Falsified (after 7 tests and 9 shrinks):
Branch Leaf 0 0 (Branch Leaf 0 0 Leaf)
Leaf
```



```
=== prop InsertValid from BSTSpec.hs:19 ===
*** Failed! Falsified (after 6 tests and 8 shrinks):
0
0
Branch Leaf 0 0 Leaf
=== prop DeleteValid from BSTSpec.hs:22 ===
*** Failed! Falsified (after 8 tests and 7 shrinks):
0
Branch Leaf (1) (Branch Leaf 0)
                                D Leaf)
=== prop UnionValid from BSTSpec.hs:25 ===
*** Failed! Falsified (after 7 tests and 9 shrinks):
Branch Leaf( 0 ) (Branch Leaf( 0 ) Leaf)
Leaf
```

Testing our tests

prop_ArbitraryValid t = valid t

prop_ShrinkValid t = all valid (shrink t)

Branch Leaf 0 0 (Branch Leaf 0 1 Leaf)
→ Branch Leaf 0 0 (Branch Leaf 0 0 Leaf)



What is the *postcondition*?

"After calling insert, we should be able to find the key inserted, and any other keys present beforehand"



What is the postcondition of **find**?

"After calling find,

—if the key is present in the tree, the result is **Just value**

—if the key is not present, the result is **Nothing**"

How can we tell this?

By construction!



prop_FindPostAbsent k t =
 find k (delete k t) === Nothing



prop_InsertInsert (k,v) (k',v') t =
insert k v (insert k' v' t)
===
if k==k' then insert k v t else
insert k' v' (insert k v t)

=== prop_InsertInsert from BSTSpec.hs:78 ===
*** Failed! Falsified (after 2 tests):
(1,0)
(0,0)
Leaf
Branch Leaf 0 0 (Branch Leaf 1 0 Leaf) /=

Branch (Branch Leaf 0 0 Leaf) 1 0 Leaf

Equivalence for trees

t1 =~= t2 =
 toList t1 === toList t2

```
prop_InsertInsert (k,v) (k',v') t =
insert k v (insert k' v' t)
=~=
if k==k' then insert k v t else
insert k' v' (insert k v t)
```


Metamorphic Testing

Montréal, QC, Canada

conjunction with ICSE 2019

May 26, 2019


```
prop_InsertModel (k,v) t =
   toList (insert k v t)
   ===
   L.insert (k,v) (toList t)
```

```
*BSTSpec> quickCheck prop_InsertModel
*** Failed! Falsified (after 13 tests and 7 shrinks):
(1,0)
Branch Leaf 1 0 Leaf
[(1,0)] /= [(1,0),(1,0)]
duplicated key
```

prop_InsertModel (k,v) t =
 toList (insert k v t)
 ===

L.insert (k,v) (deleteKey k \$ toList t)

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Proof of Correctness of Data Representations

C. A. R. Hoare

Received February 16, 1972

Summary. A powerful method of simplifying the proofs of program correctness is suggested; and some new light is shed on the problem of functions with side-effects.

1. Introduction

In the development of programs by stepwise refinement [1-4], the programmer is encouraged to postpone the decision on the representation of his data until after he has designed his algorithm, and has expressed it as an "abstract" program operating on "abstract" data. He then chooses for the abstract data some convenient and efficient concrete representation in the store of a computer; and finally programs the primitive operations required by his abstract program in terms of this concrete representation. This paper suggests an automatic method of accomplishing the transition between an abstract and a concrete program, and also a method of proving its correctness; that is, of proving that the concrete representation exhibits all the properties expected of it by the "abstract" pro-

Type of property	Number of properties
Invariant	4
Postcondition	5
Metamorphic	16
Model-based	5

Type of property	Number of properties	Bugs missed
Invariant	4	5
Postcondition	5	0
Metamorphic	16	0
Model-based	5	0

Effectiveness

prop_FindPostPresent k v t = find k (insert k v t) === Just v

Type of property	Number of properties	Bugs missed	Effectiveness
Invariant	4	5	38%
Postcondition	5	0	79%
Metamorphic	16	0	90%
Model-based	5	0	100%

=== prop_UnionPost from BSTSpec.hs:75 ===
Mean time to failure: 50.04595404595405

=== prop_InsertUnion fr
Mean time to failure

=== prop_DeleteUnion fr
Mean time to failure: 4

=== prop_UnionDeleteIns
Mean time to failure: 7

== prop_UnionUnionAsso
Mean time to failure: 8

=== prop_FindUnion from
Mean time to failure

-ogically equivalent!

c.hs:117 ===
5374626

ec.hs:145 === 696303694

BSTSpec.hs:167 === 32767233

STSpec.hs:185 === 95104895

.hs:206 === .72827

=== prop_UnionModel from pec.hs:290 ===
Mean time to failure: 8.360031368631368

```
prop_UnionPost t t' k =
  find k (union t t')
  ===
  (find k t <|> find k t')
```

```
prop_UnionModel t t' =
   toList (union t t')
   ====
   List.sort
   (List.unionBy
      ((==) `on` fst)
      (toList t)
      (toList t'))
```

Mean time to failure

Property type	Min	Max	Mean
Postcondition	9.7	160	68
Metamorphic	1	401	61.6
Model-based	5	6.5	5.8

Averaged over seven bugs, and all properties of each type that detect the bugs

Model-based

- Easier to think of than postconditions
- Require fewer properties than metamorphic approach
- Are the most effective properties
- Find bugs fastest
- Complete specification

Metamorphic

- Do not require a model
- Easiest to write
- Good effectiveness

How to Specify it!

A Guide to Writing Properties of Pure Functions.

John Hughes

Chalmers University of Technology and Quviq AB, Göteborg, Sweden.

Abstract. Property-based testing tools test software against a *specification*, rather than a set of examples. This tutorial paper presents five generic approaches to writing such specifications (for purely functional code). We discuss the costs, benefits, and bug-finding power of each approach, with reference to a simple example with eight buggy variants. The lessons learned should help the reader to develop effective property-based tests in the future.

1 Introduction

Property-based testing (PBT) is an approach to testing software by defining general properties that ought to hold of the code, and using (usually randomly) generated test cases to test that they do, while reporting minimized failing tests if they don't. Pioneered by QuickCheck¹ in Haskell [7], the method is now supported by a variety of tools in many programming languages, and is increasingly popular in practice. Searching for "property-based testing" on Youtube finds many videos on the topic—most of the top 100 recorded at developer conferences and meetings, where (mostly) other people than this author present ideas, tools and methods for PBT, or applications that make use of it. Clearly, Michał Pałka Magnus Myreen (Eds.)

Trends in Functional Programming

19th International Symposium, TFP 2019 Gothenburg, Sweden, June 11–13, 2019 Revised Selected Papers

Just submitted: How to Specify it! A Guide to Writing Properties of Pure Functions. Hope it will prove useful!

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